

(27)

Let $y(t)$ = dist. to right (m) from the equilibrium position at time t (in sec).

Then $my'' + ky = 0.$
 $2y'' + 50y = 0$
 $y'' + 25y = 0.$

A.E.

$$r^2 + 25 = 0$$

$$r^2 = -25, \quad r = \pm 5i.$$

The general soln is given by

$$y = c_1 \cos 5t + c_2 \sin 5t,$$

c_1, c_2 constants.

We are given that

$$y(0) = -1/4, \quad y'(0) = -1.$$

$$y(0) = c_1 = -1/4.$$

$$y' = -5c_1 \sin 5t + 5c_2 \cos 5t.$$

$$y'(0) = 5c_2 = -1, \quad c_2 = -1/5.$$

$$y = -\frac{1}{4} \cos 5t - \frac{1}{5} \sin 5t$$

$$= A \sin(5t + \phi)$$

$$= A (\sin 5t \cos \phi + \cos 5t \sin \phi)$$

$$A \cos \phi = -1/5$$

$$A \sin \phi = -1/4$$

$$A = \sqrt{\frac{1}{25} + \frac{1}{16}} = \sqrt{\frac{16 + 25}{25 \cdot 16}} = \frac{\sqrt{41}}{20}.$$

$$\tan \phi = \frac{-1/4}{-1/5} = 5/4.$$

ϕ is polar angle of point $(-1/5, -1/4)$ which is in 3rd quadrant.

$$\phi = \tan^{-1}(5/4) + \pi \approx 4.04.$$