

(40)
(2)

$$\begin{aligned} M'(\gamma) &= \frac{-1}{2} \frac{1}{((k-m\gamma^2)^2 + b^2\gamma^2)^{3/2}} \\ &\quad \times \{ 2(k-m\gamma^2)(-2\gamma m) + 2b^2\gamma \} \\ &= \frac{-\gamma}{(\quad)^{3/2}} \{ -2(k-m\gamma^2)m + b^2 \} \\ &= \frac{-\gamma}{(\quad)^{3/2}} \{ 2m^2\gamma^2 + b^2 - 2km \} = 0 \end{aligned}$$

When $\gamma=0$ or $2m^2\gamma^2 = 2km - b^2$

$$\gamma^2 = \frac{2km - b^2}{2m^2} = \frac{k}{m} - \frac{b^2}{2m^2}$$

$$\gamma = \sqrt{\frac{k}{m} - \frac{b^2}{2m^2}}$$

NOTE: For underdamped case $b^2 < 4km$

$M(\gamma)$ has maximum if $b^2 < 2km$.

In this case $b^2 < 2km < 4km$ and the system is underdamped. In this case,

$$\frac{1}{2\pi} \gamma_r = \frac{1}{2\pi} \sqrt{\frac{k}{m} - \frac{b^2}{2m^2}} \quad \text{is called}$$

the

resonance frequency and the system is said to be at resonance.