

We solve this first order linear DE in Y .

(21)

An integrating factor is $\int 2/s ds$

$$\mu(s) = e^{\int 2/s ds} = e^{2 \ln s} = s^2.$$

$$\begin{aligned} \frac{d}{ds} (s^2 Y) &= 2sY + s^2 Y' \\ &= s^2 \left(Y' + \frac{2}{s} Y \right) \\ &= s^2 \left(\frac{2}{s^2} \right) = 2. \end{aligned}$$

so

$$\frac{d}{ds} (s^2 Y) = 2$$

$$s^2 Y = 2s + C$$

$$Y = \frac{2}{s} + \frac{C}{s^2}$$

$$y = \mathcal{L}^{-1}\{Y\} = 2 + ct$$

$$y(0) = 2.$$

$$y'(t) = c, \quad y'(0) = -1 \Rightarrow c = -1 \quad \&$$

$$\boxed{y = 2 - t}$$