

$$= \int_0^{\infty} f(v) e^{-sv} e^{-sa} dv$$

$$= e^{-sa} \int_0^{\infty} e^{-sv} f(v) dv = e^{-sa} F(s). \quad \square$$

Corollary, Let $h(t) = g(t+a)$. Then

$$\mathcal{L}\{h(t-a)u(t-a)\} = \mathcal{L}\{g(t)u(t-a)\}$$

$$= e^{-as} \mathcal{L}\{h(t)\}$$

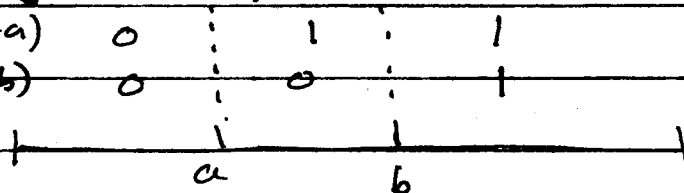
$$= e^{-as} \mathcal{L}\{g(t+a)\}$$

$$\boxed{\mathcal{L}\{g(t)u(t-a)\} = e^{-as} \mathcal{L}\{g(t+a)\}}$$

Let $0 \leq a < b$.

$$u(t-a) = H(t-a)$$

$$u(t-b) = H(t-b)$$



$$u(t-a) - u(t-b) = H(t-a) - H(t-b) = \begin{cases} 1 & \text{if } a < t < b \\ 0 & \text{otherwise} \end{cases}$$

Example

