

The general soln is given by

(11)

$$y = C_1 \left(1 + x^2 + \frac{1}{2}x^4 + \dots \right) \\ + C_2 \left(x + \frac{2}{3}x^3 + \frac{4}{15}x^5 + \dots \right)$$

for any constants C_1, C_2 .

(b) Repeat problem but find a general formula for the coefficients.

$$y = \sum_{n=0}^{\infty} a_n x^n.$$

We found $a_{n+2} = \frac{2a_n}{n+2}$ for $n \geq 0$.

For $y_1, a_0, a_1, a_2, \dots$

$$a_2 = a_0$$

$$a_3 = \frac{2}{3} a_1$$

$$a_4 = \frac{2}{4} a_2 = \frac{1}{2} a_0$$

$$a_5 = \frac{2}{5} a_3 = \frac{2}{5} \cdot \frac{2}{3} \cdot a_1$$

$$a_6 = \frac{2}{6} a_4 = \frac{1}{3} \cdot \frac{1}{2} \cdot a_0$$

$$a_7 = \frac{2}{7} a_5 = \frac{2}{7} \cdot \frac{2}{5} \cdot \frac{2}{3} \cdot a_1$$

$$a_8 = \frac{2}{8} a_6 = \frac{1}{4} \cdot \frac{1}{3} \cdot \frac{1}{2} \cdot a_0$$