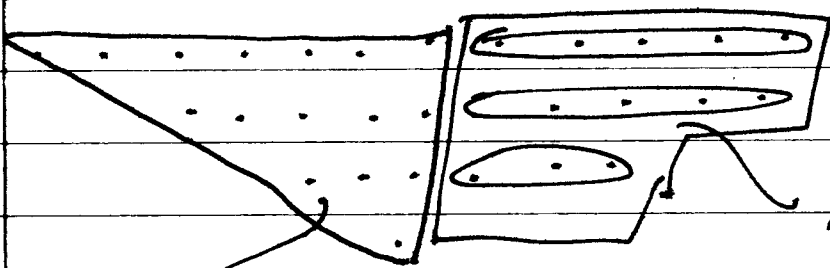


We obtain

$$d_k = (2k-1), d_{k-1} = (2k-3), \dots, d_{k-6} = 2k-6 - (2k+1) \\ \dots, \alpha_1 = (2_1 - (2k-1)), \text{ and} \\ d_k \geq d_{k-1} \geq \dots \geq d_2 \geq \alpha_1 = 0.$$



pts into at most  
k parts

$$q^{1+3+\dots+(2k-1)} = q^{\frac{k^2}{2}} \quad \frac{1}{(q)_{2k}}$$

Let  $p_k(R, n) = \#$  of partitions of  $n$  into  $k$  parts  
in which difference between parts  $\geq 2$ .

Let  $p(R, n) = \#$  of partitions of  $n$  in which diff between  
parts  $\geq 2$ .

$$\text{Then } \sum_{n \geq 0} p_k(R, n) q^n = \frac{q^{\frac{k^2}{2}}}{(q)_{2k}}$$

$$\sum_{n \geq 0} p(R, n) q^n = \sum_k \left( \sum_{n \geq 0} p_k(R, n) q^n \right) = \sum_{k=0}^{\infty} \frac{q^{\frac{k^2}{2}}}{(q)_{2k}}$$

EX:  $\sum_{n \geq 0} \frac{q^{\frac{n^2}{2}}}{(q)_{2n}}$  is G.F. for partitions into parts  $\geq 2$   
in which diff. between parts  $\geq 2$ .

Cor

(1) The number of ptns of  $n$  in which diff. between parts  $\geq 2$   
= The number of ptns of  $n$  into parts  $\equiv 1, 4 \pmod{5}$ .

(2) The number of ptns of  $n$  in which diff. between parts  $\geq 2$  & no ones  
= The number of ptns of  $n$  into parts  $\equiv 2, 3 \pmod{5}$ .